CLASSICAL PROPUSITIONAL CALCULUS

Symbols Variables P= { Pn: n E w} Connectives not, and, or --Punctuation), (String is a finite sequence of symbols Wff. is a meaningful'string

F = {Wff}.

7

CHARACTERISTIC ALGEBRAS

John is to replace $f_{B_2} \in B_2^F$ by $f_A \in A^F$ Wiff ϕ is satisfied by f_A iff $f_A(\phi) \in D$ set of designated elements of A

\$\phi\$ verified by \$R\$ (1.0. is \$R-Valid)

Iff \$\forall f_A(\phi) \in D)\$

An algebra A is characteristic for an abstract logical calculus if theoremhood can be identified with A-validity.

Theorem 9f B is an arbitrary Boolean Algebra a formula of CPC is B- Valid iff the formula is B2- Valid.

- (1) B-Valid -> B2-Valid

 B always has B2 as a sub-algebra.
- (2) B2-Valid -> B-Valid.

 Assume \$\phi\$ us B2-Valid out

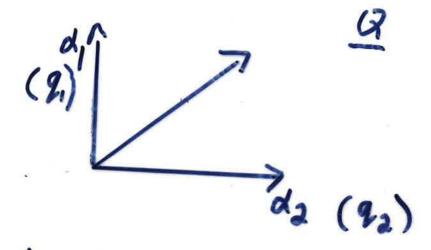
 not B-Valid

 So \$\exists f_B(\phi) \neq 1.

Sunce fB (4) +1 fB(nd) #0 so by Ultrafilter Theorem fo(2 \$) is contained in some Ulf of B :. Wy Homomorphism Therem fB(2 \$) 1 under some Romomorphism H: B-> B= · · · FB(\$) HO which implies a B2-realization f = HofB for which f(\$)=0, contrary to hypothesis - Result follows.

CONNECTIVES IN QM

DISTUNCTION :



Pi: state of system is associated with Kayd,
Pa:

Pron Pa: state of system in which result of measurement is 2, un 92

=D state-vorter Pres in Punear span
of 2, 2a

QUANTUM NEGATION

of measurement never yorlds q

Compare classical negation:

7 P: State is such that result of measurement is not always 2

QUANTUM CONJUNCTION

P, & Pa = DE 7 (7P, Or 7P2)

Ex P. sous a yields 2, on to on measurement Pa ... 920183 .

P. R.B. . 22 only.

Proof that $Val[\{i\}]_{g}^{\phi} = Val[\{i\}]_{g}^{\phi}$ An observable Q is a map $Q: \{\Delta\} \rightarrow \{P\}$ $\Delta \mapsto l_{Q}(\Delta)$ Now Proof $[\Delta]_{f}^{\phi} = lnob[f'(\Delta)]_{g}^{\phi}$ Assume $(functional\ Composition\ Painciple)$

Assume (functional composition principle)

Val [D] f(a) = Val [f'(A)] g

The ((a) = (a) =

Take $f(Q) = \chi_{\Delta}(Q) = P_{Q}(\Delta)$ Then $Val [\{ii\}]_{PQ(\Delta)}^{\phi} = Val [\chi_{\Delta}^{-1}\{i\}]_{Q}^{\phi}$ Result follows if we take $\Delta = \{\lambda\}$

THE TWO-COLOUR THEOREM

On a Rypensphere in a Enclidean Space of three or more dumansions it is not possible to colour every point with either & 2 colours, sad & Whee, so that to every onthogonal N-tuple of points anely one is colounal ned.